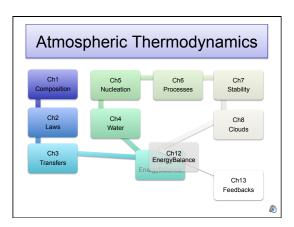
Climate Sciences: Atmospheric Thermodynamics

Instructor: Lynn Russell, NH343 http://aerosol.ucsd.edu/courses.html Text: Curry & Webster

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Course Principles

- · Green classroom
 - Minimal handouts, optional paper text, etc.
- · Respect for learning
 - On time, on schedule: quizzes
 - No chatting (in class), no cheating
- · Focused exams
 - Core principles not algebra
- "Office hours" <u>help</u> on homework, projects
- Team learning by projects
 - Bring different backgrounds to common topics

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Homework Schedule

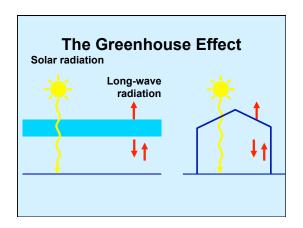
Email Single PDF to Imrussell@ucsd.edu

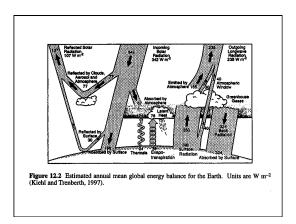
- Due Oct. 13 (Monday, 12 noon)
- Due Oct. 20 (Monday, 12 noon)
- Ch. 2, Problem 2
- Due Nov. 3 (Monday, 12 noon)
- Due Nov. 10 (Monday, 12 noon)
- Due Nov. 17 (Monday, 12 noon)
- Ch. 5, Problem 3, 7 (erratum in 7d)

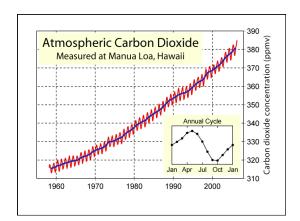
 Midterm Nov. 19 (Wednesday, in class)
- Due Nov. 24 (Monday, 12 noon)
- Due Dec. 1(Monday, 12 noon)
- Ch. 7, Problem 3 (not graded, outline approach only, discuss)

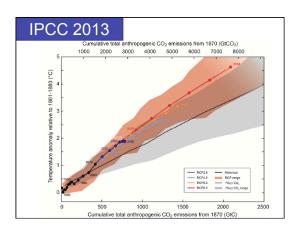
What do we learn in Ch. 1?

- What P, T, U are for a fluid
- What an ideal gas is
- How P, T, v relate for an ideal gas (and we call this relationship an equation of state)
- What chemical components constitute the atmosphere (for homosphere <110 km)
- What the hydrostatic balance is
- How p, T vary with z for observed, "standard," isopycnic, isothermal, constant lapse-rate atmospheres







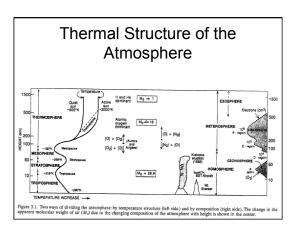


Review Topics in Ch. 1

- · Thermodynamic quantities
- Composition
- Pressure

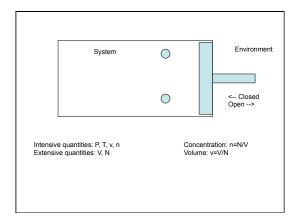
Curry and Webster, pp. 1-17 Feynman, Book I, ch. 39

- Density
- Temperature
- Kinetic Theory of Gases



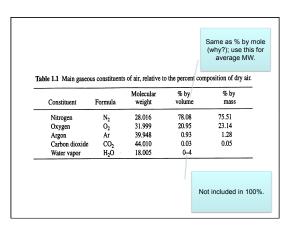
Thermodynamic Quantities

- · Classical vs. Statistical thermodynamics
- · Open/closed systems
- Equation of state f(P,V,T)=0
- Extensive/intensive properties
- Thermal, engine, heat/work cycles



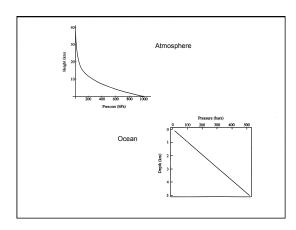
Composition

- Structure
 - Comparison to other planets
- N_2 , O_2 , Ar, CO_2 , H_2O : 110 km constitute 99%
- · Water, hydrometeors, aerosol



Pressure

- · Force per unit area
- 1 bar = 10⁵ Pa; 1 mb = 1 hPa; 1 atm = 1.013 bar
- · Atmosphere vs. Ocean



Pressure

- · Force per unit area
 - 1 bar = 105 Pa:
 - -1 mb = 1 hPa;
 - 1 atm = 1.013 bar

Density

- Specific volume: v=V/m
 - 0.78 m³ kg-1 for air
- Density: ρ=m/V
- 1.29 kg m⁻³ for air



Geopotential Height (km) polar winter - standard atmosphere -20 Temperature (°C)

Figure 1.7 Vertical temperature structure in the atmosphere below about 50 km. Temperature decreases with height in the troposphere, except for the polar winter, where surface temperatures are very low, causing a temperature inversion near the surface (U.S. Standard Atmosphere, 1976).

Temperature

- "Zeroeth" Law of Thermodynamics
 - Equilibrium of two bodies with third
 - Allows universal temperature scale
- Temperature scale
- Two fixed points: Kelvin, Celsius
- Thermometer
- Lapse Rate $\Gamma = -\partial T/\partial z$
- Change in temperature with altitude
 Typically Γ=6.5 K/km
- Temperature inversion Γ <0
 - Boundary layer "cap"
 - Tropopause between troposphere and stratosphere

History of the Standard Atmosphere

- With a little digging, you can discover that the Standard Atmosphere can be traced back to 1920. The constant lapse rate of 6.5° per km in the troposphere was suggested by Prof. Toussaint, on the grounds that

 what is needed is merly a law that can be conveniently applied and which is sufficiently in concordance with the means adhered to. By this method, corrections due to temperature will be as small as possible in calculations of airplane performance, and will be easy to calculate.

 The deviation is of come click in the control of the
 - will be easy to calculate. ... The deviation is of some slight importance only at altitudes below 1,000 meters, which altitudes are of little interest in aerial navigation. The simplicity of the formula largely compensates this inconvenience.
- The above quotation is from the paper by Gregg (1920). The early motivations for this simplified model were evidently the calibration of aneroid altimeters for aircraft, and the construction of firing tables for long-range artillery, where air resistance is important.
- Unfortunately, it is precisely the inaccurate region below 1000 m that is most important for refraction near the horizon. However, the Toussaint lapse rate,
- cannot be altered: all revisions of the Standard Atmosphere have preserved it. Therefore, the Standard Atmosphere is really inappropriate for astronomical refraction calculations. A more realistic model would include the diurnal changes in the boundary layer; but these are still so poorly understood that no satisfactory basis seems to exist for realistic refraction tables near the horizon.

International Standard Atmosphere

The ISA model divides the atmosphere into layers with linear temperature distributions, [2] The other value are computed from basic physical constants and relationships. Thus the standard consists of a table of values at various altitudes, plus some formulas by which those values were derived. For example, at sea level the standard gives a pressure of 1.013 bar and a temperature of 15°C, and an initial layer rate of -6.5°C/Am. Above 12km the tabulated temperature is essentially constant. The tabulation continues to 18km where the pressure has fallen to 0.075 bar and the temperature 5.6.5°C/3[3]4]

Layer	Level Name	Base Geopotential Height h (in km)	Base Geometric Height z (in km)	Lapse Rate (in °C/km)	Base Temperature T (in °C)	Base Atmospheric Pressure p (in Pa)
0	Troposphere	0.0	0.0	-6.5	+15.0	101,325
1	Tropopause	11.000	11.019	+0.0	-56.5	22,632
2	Stratosphere	20.000	20.063	+1.0	-56.5	5,474.9
3	Stratosphere	32.000	32.162	+2.8	-44.5	868.02
4	Stratopause	47.000	47.350	+0.0	-2.5	110.91
5	Mesosphere	51.000	51.413	-2.8	-2.5	66.939
6	Mesosphere	71.000	71.802	-2.0	-58.5	3.9564
7	Mesopause	84.852	86.000	-	-86.2	0.3734

- * U.S. Extension to the ICAO Standard Atmosphere, U.S. Government Printing Office, Washington, D.C., 1958.
 * U.S. Standard Atmosphere, 1962, U.S. Government Printing Office, Washington, D.C., 1962.
 * U.S. Standard Atmosphere Supplements, 1966, U.S. Covernment Printing Office, Washington, D.C., 1966.
 * U.S. Standard Atmosphere, 1976, U.S. Government Printing Office, Washington, D.C., 1976.

Geopotential Height

Geopotential height is a vertical coordinate referenced to Earth's mean sea level — an adjustment to geometric height (elevation above mean sea level) using the variation of gravity with latitude and elevation. Thus it can be considered a "gravity-adjusted height." One usually speaks of the geopotential height of a certain pressure level, which would correspond to the geopotential height necessary to reach the given pressure.

At an elevation of h, the **geopotential** is defined as

$$\Phi = \int_0^h g(\phi, z) dz,$$

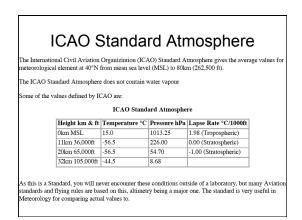
where $g(\phi,z)$ is the acceleration due to gravity, ϕ is latitude, and z is the geometric elevation.

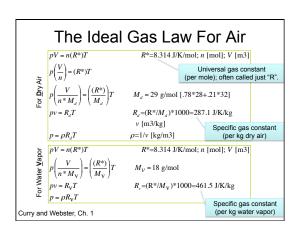
Thus, it is the gravitational potential energy per unit mass at that level. The geopotential height is

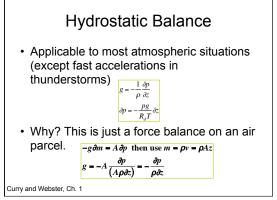
$$Z_g = \frac{\Phi}{g_0} \,,$$

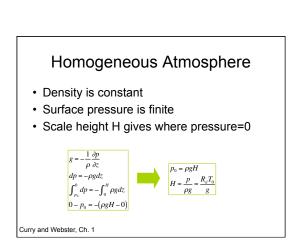
where g_0 is the standard gravity at mean sea level.

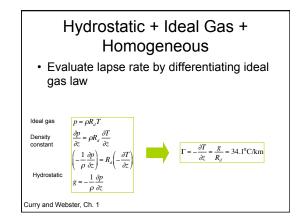
Geophysical scientists often use geopotential height rather than geometric height, because doing so in many cases makes analytical calculations more convenient. For example, the primitive equations which weather forecast models solve are more easily expressed in terms of geopotential than geometric height. Using the former eliminates centrifugal force and air density (which is very difficult to measure) in the

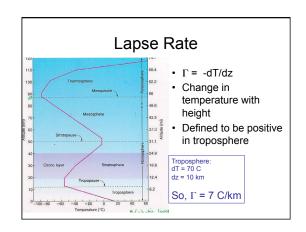












Hydrostatic Equation (1)

• Hydrostatic Balance (1.33)

$$g = -\frac{1}{\rho} \frac{\partial p}{\partial z}$$

Geopotential Height (1.36a)

$$Z = -\frac{1}{g_0} \int_0^z g dz$$

· Homogeneous atmosphere (1.38)

$$p_0 = \rho g H$$
[N B $\rho = constan$

$$\frac{\partial p}{\partial z} = \rho R_d \frac{\partial T}{\partial z}$$
[N.B. ideal gas]

[N.B.
$$\rho = \text{constant}$$
]

$$H = \frac{R_d T_0}{g} = 81$$

$$H = \frac{R_d T_0}{g} = 8 \text{ km}$$

$$\Gamma = -\frac{\partial T}{\partial z} = \frac{g}{R_d} = 34.1^{\circ} \text{C km}^{-1}$$

Hydrostatic Equation (2)

· Isothermal Atmosphere (1.42)

$$\partial p = -\frac{pg}{R_d T} \partial z$$

$$p = p_0 \exp\left(\frac{-z}{H}\right)$$
 for $H = \frac{RT}{g}$

• Constant Lapse Rate (1.48)

$$\frac{dp}{p} = -\frac{g}{R_d} \frac{dz}{T_0 - \Gamma z}$$
[N.B. Γ = constant]

$$[N.B. \Gamma = constant]$$

$$p = p_0 \left(\frac{T}{T_0}\right)^{g/R_d \Gamma}$$

Homework Schedule

Email Single PDF to Imrussell@ucsd.edu Reminders

- Due Oct. 13 (Monday, 12 noon)
- Due Oct. 20 (Monday, 12 noon) - Ch. 2, Problem 2
- Due Nov. 3 (Monday, 12 noon)
- Ch. 4, Problem 4, 5
- Due Nov. 17 (Monday, 12 noon)
- Ch. 5, Problem 3, 7 (erratum in 7d)

 Midterm Nov. 19 (Wednesday, in class)
- Due Nov. 24 (Monday, 12 noon)

- Due Dec. 1(Monday, 12 noon)

 Ch. 7, Problem 3 (not graded, outline approach only, discuss)

Quiz Ch. 1

- · Write the ideal gas law for dry air.
- · What is the homosphere?
- · What causes pressure?
- · How does pressure vary with increasing altitude?
- · Define lapse rate.
- · Write the hydrostatic balance.

N.B. If you use a sign convention different from the text, please state it Curry and Webster, Ch.

Kinetic Theory of Gases

- · What is the pressure of a gas?
- · What is the temperature of a gas?
- Pressure-volume-temperature relationship(s)
- · How does pressure (and volume) relate to energy?
- Kinetic energy
- · Internal energy
 - The "fine print"

