

# 1 ROAST PROJECT – SIO 217A

---

2 Felipe Mejia, Homa Naeimi, Handa Yang, Xiaohui Zhong

## 3 1. Introduction

4 In a normal atmosphere, a large fraction of incoming solar energy is absorbed by the  
5 ground and is converted to heat. As a result, the temperature of the atmospheric  
6 surface layer rises. The warm air then rises, expands and cools. In general, within the  
7 troposphere, temperature decreases as height increases. This relation is described by  
8 temperature lapse rate which is defined as (Curry & Webster, 1999):

$$\Gamma = -\frac{dT}{dz}$$

9 A temperature inversion occurs when there is deviation from this pattern and the  
10 normal vertical temperature gradient is inverted (Curry & Webster, 1999). During  
11 inversion, a warm, less dense layer of air covers a denser cold layer underneath and  
12 creates atmospheric stability. Temperature inversions can be categorized into four  
13 different types: ground, marine, subsidence, and frontal (NOAA).

14 Several meteorological conditions may cause temperature inversion. For example,  
15 during the night, the ground acts as a heat sink. The surface layer of the atmosphere  
16 loses heat to the ground while above layers retain the heat they absorbed from the  
17 ground during the day (Salby, 2012). As a result, a cold layer of air develops  
18 underneath a warmer layer, which forms ground inversion. Another scenario is often  
19 observed on coastal areas, where cold water acts as a heat sink and decreases air  
20 temperature at lower layers, while above layers maintain a higher temperature forming  
21 the marine inversion layer. One such situation often occurs in southern California  
22 because of the cool ocean water, as well as the warm inland temperatures (Antoine  
23 Badan-Dangon, 1991).

24 Temperature inversion is followed by various consequences, such as freezing rain.  
25 When there is a shallow inversion in the presence of snow aloft, the snow melts as it  
26 moves through the warm inversion layer and is later super-cooled as it passes through  
27 near the surface cold air masses. The super-cooled drops then become ice when they  
28 land on the ground and other surfaces (Jones, 1998). Sometimes intense  
29 thunderstorms are created due to the intense energy that is released after an inversion  
30 layer is broken and normal convection patterns reform (Schaefer, 1986).

31 Temperature inversion plays a significant role in trapping pollution over megacities  
32 by blocking atmospheric flows and causing the atmosphere to become stable. When  
33 pollutants from vehicles and industry are emitted into the air, the inversion traps the  
34 particles and pollutants near the ground. As a result, smog, which is a gray haze of  
35 dust, auto exhaust, and industrial manufacturing, covers the cities, leading to poor air  
36 quality (Edinger, 1973). Because temperature inversion has such significant effects on  
37 air quality, it is important to better understand this phenomenon, its causes, and  
38 consequences.

39 In this study, a simplified atmospheric model based on the air parcel model  
40 described in Pruppacher & Klett (1996) is used to study the effects of temperature  
41 inversion on atmospheric convection. Three modeling cases were analyzed. The first  
42 case involved a control run without modifying model parameters beyond their default  
43 values. The following two cases involved the addition of a temperature inversion at 1.00  
44 km and 0.25 km, respectively. The results from the last two cases were compared  
45 against the control run in order to infer variations in atmospheric behaviors in the  
46 presence of different temperature inversions.

## 47 2. Model description

48 For the purposes of our model, an “air parcel” is defined as an infinitesimal, well-  
49 defined body of air that does not readily mix with the surrounding air, and its  
50 temperature is assumed to be generally uniform (Spellman, 2012). To initialize the  
51 model, a parcel of air is given an initial temperature and humidity, and its ascent in the  
52 atmosphere is described by solving the buoyancy (Eqn. 1) and energy conservation  
53 (Eqn. 2) equations:

54 Equation 1- Buoyancy Force

$$F_{buoyancy} = g \left( \frac{T_{parcel} - T_{ambient}}{T_{ambient}} - w_l \right)$$

55

56 Equation 2 - Energy Conservation Equation

$$\left( c_p + L_{lv} \frac{dw_s}{dT} \right) dT = -gWdt$$

57

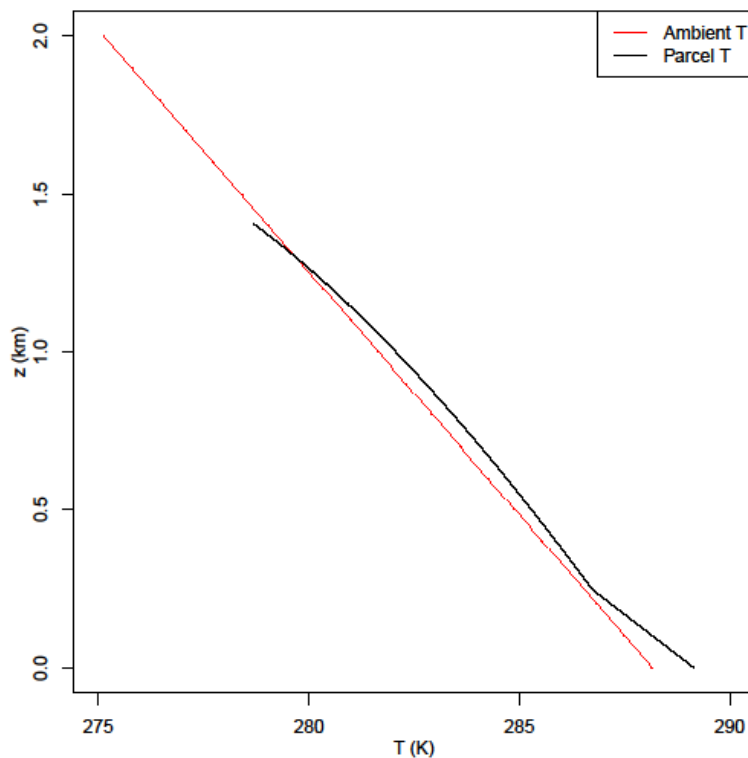
58 The following assumptions are made in order to simplify the model: (1) there is no  
59 drag force on the parcel due to turbulence along its edges, (2) the ambient temperature  
60 profile prior to the temperature inversion (which is described by a dry adiabatic lapse  
61 rate and is capped at the surface temperature) is described by the US standard  
62 atmosphere, with a surface temperature of 288 K at sea level and a lapse rate of 6.5  
63 K/km, (3) the ambient humidity profile is 80% relative humidity throughout, (4) the  
64 parcel’s ascent is an adiabatic process, (5) the parcel does not mix, (6) the parcel does  
65 not disturb the environment, and (7) the parcel is in mechanical equilibrium with the  
66 environment (pressure in the parcel is equal to the ambient pressure).

67 Although this air parcel model is useful for demonstrating concepts, the  
68 simplifications made introduce a degree of inaccuracy. Since the entrainment of  
69 ambient air is neglected, the air parcel is assumed to be a closed system, which may  
70 lead to higher parcel liquid water content (failed to account for the drying effects of  
71 entraining relatively dry ambient air). Additionally, the assumption that the parcel  
72 ascension is adiabatic may cause the modeled parcel height to be much higher than  
73 actual observations show (Pruppacher & Klett, 1996). The simplified air parcel model

74 also does not account for heating due to incoming short and long wave radiation, or  
75 cooling due to radiative losses to the environment.

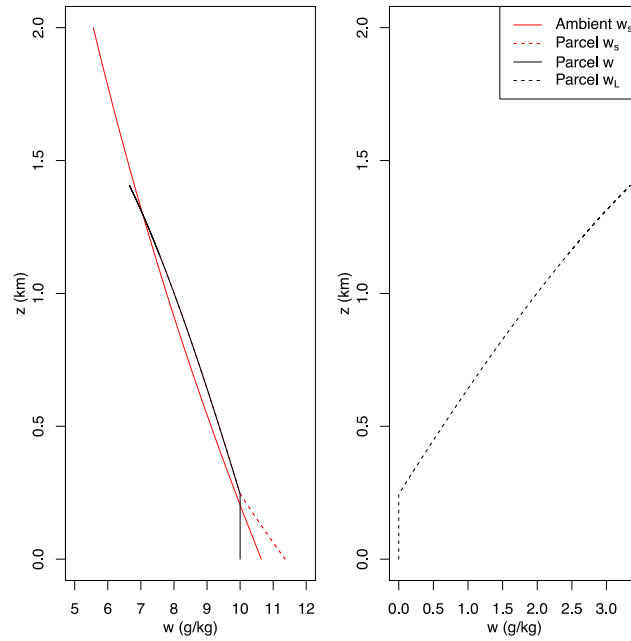
### 76 3. Results & Discussion

77 From the three cases, it was observed that the temperature inversion limited the  
78 parcel height. In the first modeled atmosphere, without a temperature inversion, the  
79 parcel's temperature is decreasing. Close to the surface it begins by following the dry  
80 adiabatic lapse rate. This is illustrated in figure 1. The parcel begins rising until it  
81 reaches about 0.25 km, at which point it reaches its lifting condensation level (LCL) as  
82 seen in figure 2. This is the point at which the parcel is fully saturated and follows the  
83 wet adiabat. Because the parcel is warmer than the ambient temperature, it continues to  
84 rise due to its buoyancy force. It continues rising until it reaches the mixing height,  
85 which is the point at which the parcel temperature intersects the ambient temperature  
86 and only goes slightly higher due to momentum. This maximum height was observed to  
87 be about 1.40 km.



88

89 **Fig. 1** Parcel height versus parcel temperature (in black) and ambient height versus temperature (in red)  
90 for an atmosphere without a temperature inversion.

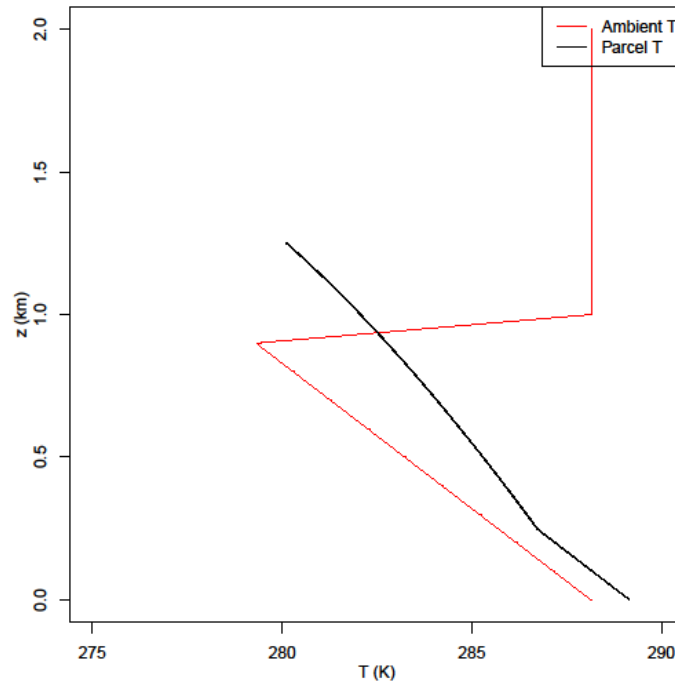


91

92 **Fig. 2** Height versus ambient saturation pressure, parcel saturation pressure and parcel mixing ratio.

93 The addition of a temperature inversion to the model caused the parcel to stop rising  
 94 much closer to the surface than without the temperature inversion. With an inversion at  
 95 1.00 km, the parcel reached a maximum height around 1.25 km as shown in figure 3.  
 96 The parcel stops accelerating soon after reaching its mixing height.

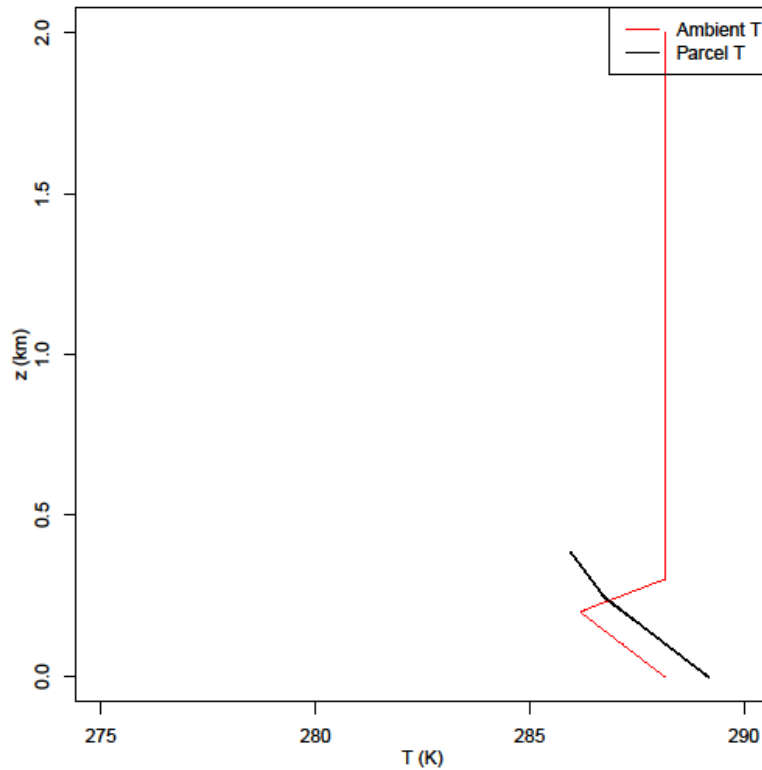
97



98

99 **Fig. 3** Parcel height versus parcel temperature (in black) and ambient height versus temperature (in red)  
 100 for an atmosphere with a temperature inversion at a height of 1 km.

101 The temperature inversion at 0.25 km limited the parcel height even further. In this  
 102 atmosphere, the parcel height does not go beyond 0.40 km, as seen in figure 4. As in  
 103 the previous two cases, the parcel quickly stops accelerating after it reaches the mixing  
 104 height, suggesting that the point where the parcel reaches the mixing height controls the  
 105 maximum parcel height.



106

107 **Fig. 4** Parcel height versus parcel temperature (in black) and ambient height versus temperature (in red)  
 108 for an atmosphere with a temperature inversion at a height of 250 m.

109 In the three graphs, as the parcel increases in height, its temperature decreases.  
 110 Close to the surface, the three cases began by following the dry adiabat until they  
 111 reached the LCL. After the LCL, the three cases began to deviate from each other.  
 112 Without a temperature inversion, the difference in lapse rate between the parcel and the  
 113 ambient lapse rate is very small throughout the parcel's ascent, so the parcel continues  
 114 rising to very high altitudes. With a temperature inversion added, the parcel begins to  
 115 lose its buoyancy force as it reaches the temperature inversion and decelerates until it  
 116 can no longer continue rising. This is because, after the temperature inversion, ambient  
 117 temperature rises which quickly leads to the ambient temperature to be higher than that  
 118 of the parcel. Once the parcel is cooler than ambient temperature it no longer has the  
 119 buoyancy force to continue rising so it only rises slightly more due to its momentum.  
 120 The mixing ratio was found to be unaffected by the addition of the inversion, suggesting  
 121 that the inversion only affects the parcel's height. Table 1 demonstrates variations in the  
 122 mixing height of the three different cases.

123 **Table 1** Parcel mixing and maximum heights for the three different cases

	No Temperature Inversion	Temperature inversion at 1.00 km	Temperature inversion at 0.25 km
Parcel Mixing Height	1.25 km	0.90 km	0.30 km
Parcel Maximum Height	1.40 km	1.25 km	0.40 km

124 As seen in the three modeled atmospheres, the inversion limits atmospheric mixing.  
125 The warm inversion layer acts as a lid, making it difficult for the cold air below the  
126 inversion to rise. In an atmosphere, such as the one in the control case, pollutants are  
127 able to disperse up to 1.40 km, making it more difficult for high concentrations of  
128 pollution to accumulate. In this atmosphere, pollution can spread over a larger portion of  
129 the atmosphere, so more pollution is needed to reach high concentrations. In addition to  
130 this, more of the pollution is located at higher altitudes, so the surface air quality is  
131 improved. Similarly, for fog to develop, more water must evaporate to be able to  
132 saturate the larger portion of the atmosphere. The fog that does develop in this  
133 atmosphere is also located at higher altitudes. With the addition of temperature  
134 inversions, the parcel height is capped at 1.25 km and 0.40 km, respectively. This  
135 greatly reduces the amount of pollutants needed to create smog. This is the case in Los  
136 Angeles where a temperature inversion, like the case with an inversion at 1.00 km,  
137 keeps pollution closer to the surface, thus decreasing air quality. Higher concentrations  
138 of pollution are reached because the pollution is trapped by the temperature inversion.  
139 In San Diego, a temperature inversion, like the one modeled with an inversion at 1.00  
140 km, sometimes develops and leads to dense fog close to the surface. This fog develops  
141 because less water is needed to saturate the capped atmosphere. From comparing the  
142 two cases with temperature inversions, it is possible to see that the lower the inversion  
143 the lower the amount of atmospheric mixing. This reduction in mixing means that the  
144 lower the temperature inversion the higher the likelihood of fog or smog to develop.

#### 145 **4. Conclusion**

146 A parcel model was developed and run for three different cases of atmospheric  
147 temperature inversions. The three cases were for an atmosphere without a temperature  
148 inversion, with one at 1.00 km and with one at 0.25 km. The three cases were picked to  
149 compare the effects of a temperature inversion, and they demonstrated how the warm  
150 inversion layer reduced the buoyancy force acting on the parcel. The warm inversion  
151 layer was found to cap the maximum height of the parcel and reduce atmospheric  
152 mixing. This in turn leads to environmental effects such as freezing rain, fog and smog.

153

154 **Appendix A – Nomenclature**

155

156 F – Force [N]

157 g – Gravity of Earth [ $9.81 \text{ m s}^{-2}$ ]

158 T – Temperature [K]

159  $w_l$  – Liquid water mixing ratio [ $\text{kg}_{\text{H}_2\text{O}} \text{ kg}^{-1}_{\text{dry air}}$ ]

160  $w_s$  – Saturation mixing ratio [ $\text{kg}_{\text{H}_2\text{O}} \text{ kg}^{-1}_{\text{dry air}}$ ]

161  $c_p$  – Specific heat capacity at constant pressure [ $\text{J kg}^{-1} \text{ K}^{-1}$ ]

162  $L_v$  – Latent heat of vaporization of water [ $2.27 \times 10^6 \text{ J kg}^{-1}$ ]

163 W – Vertical velocity of air parcel (dz/dt) [ $\text{m s}^{-1}$ ]



164 **Works Cited**

165 Badan-Dangon, A., Dorman, C. E., Merrifield, M. A., & Winant, C. D. (1991). The lower  
166 atmosphere over the Gulf of California. *JOURNAL OF GEOPHYSICAL RESEARCH* , 16,877–  
167 16,896.

168 Curry, J. A., & Webster, P. J. (1999). *Thermodynamics of Atmospheres & Oceans*. ACADEMIC  
169 PRESS.

170 Edinger, J. G. (1973). Vertical distribution of photochemical smog in Los Angeles basin.  
171 *Environmental Science and technology* , 242-252.

172 Jones, K. F. (1998). A simple model for freezingrain ice loads. *Atmospheric Research* , 87-97.

173 NOAA. (n.d.). Retrieved 11 14, 2012, from  
174 <http://www.wrh.noaa.gov/slc/climate/TemperatureInversions.php>

175 Pruppacher, H. R., & Klett, J. D. (1996). *Microphysics of Clouds and Precipitation*. Dordrecht:  
176 Kluwer Academic Publishers.

177 Salby, M. L. (2012). *Physics of the atmosphere and climate* . New York: Cambridge University  
178 Press.

179 Schaefer, J. T. (1986). Severe Thunderstorm Forecasting: A Historical Perspective. *Weather  
180 and Forcasting* , 164-189.

181 Spellman, F. R. (2012). *Environmental Impacts of Hydraulic Fracturing*. Boca Raton: Taylor &  
182 Francis Group.